



# Distributed Control of AC/DC Microgrid Voltage Containing EVs

Meiqin Mao  
Hefei University of Technology





# Outlines

1

Introduction

2

Relationship between voltage and power  
incensement in AC&DC-HMG

3

Distributed voltage regulation algorithm

4

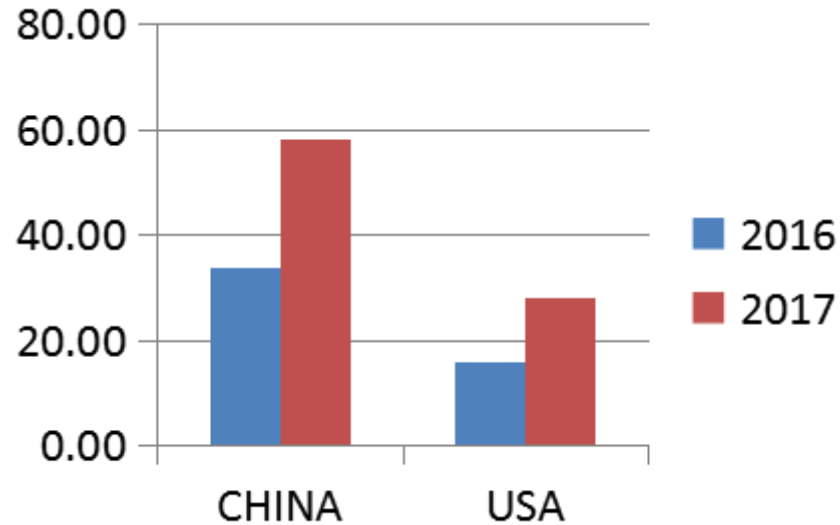
Simulation results and discussion



## Current status of electric vehicles

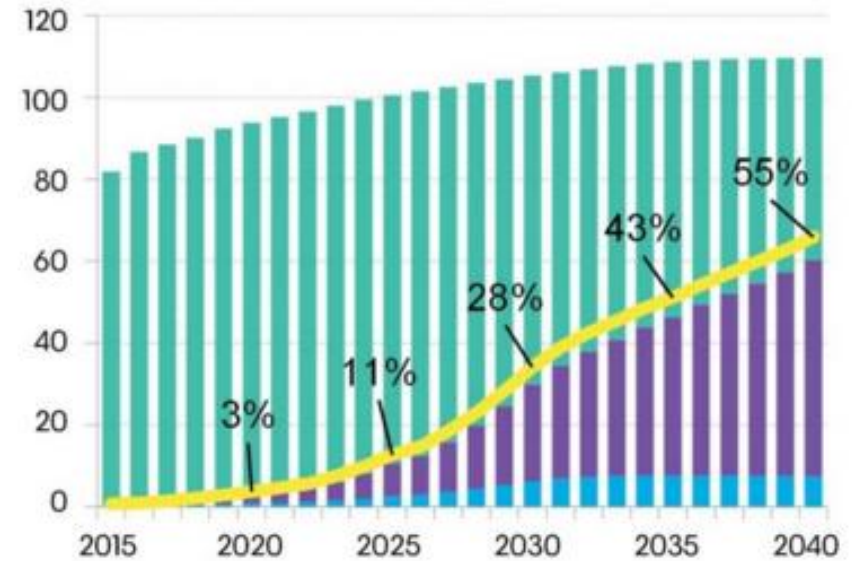
Annual sales of EVs In China

Ten thousand



(2015-2040) Annual sales volume and forecast of global vehicle

Million



EVs sales

Total vehicle sales



## Challenges of EVs integration into power system



large-scale EVs integration



Voltage  
fluctuations

Frequency  
fluctuations

Grid harmonic  
distortion

Other  
problems



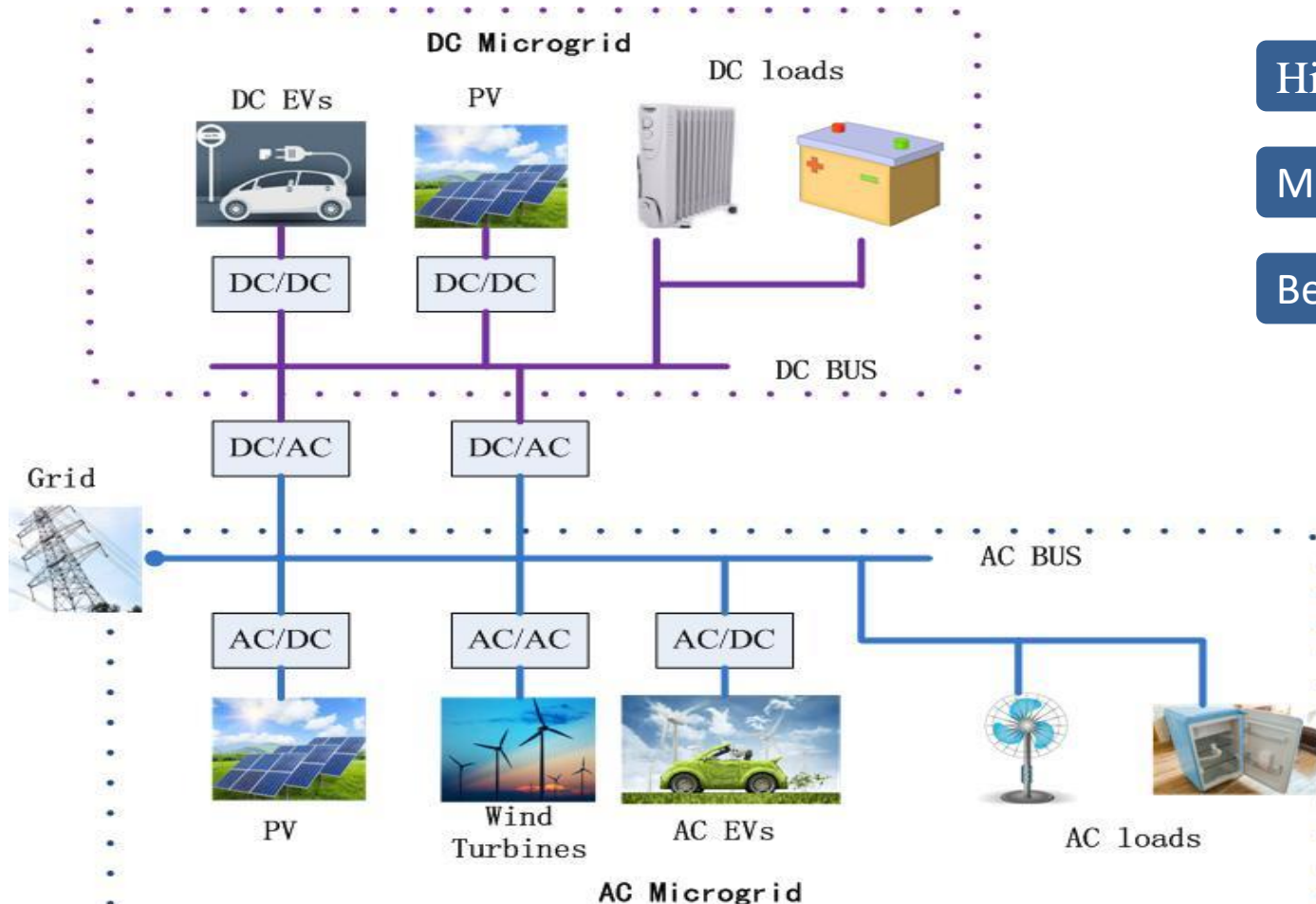
2019-Disordered charging

2019 Fort Collins Symposium on  
Microgrids





## AC&DC hybrid microgrid



Higher efficiency

More reliable

Better Expandability



# Outlines

1

Introduction

2

Relationship between voltage and power  
incensement in AC&DC-HMG

3

Distributed voltage regulation algorithm

4

Simulation results and discussion



## Relationship between Voltage Deviation and Power Increment in AC-MGs

In MGs:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} \frac{\partial P}{\partial \theta} & \frac{\partial P}{\partial U} \\ \frac{\partial Q}{\partial \theta} & \frac{\partial Q}{\partial U} \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta U / U \end{bmatrix} = \begin{bmatrix} M & N \\ K & L \end{bmatrix} \begin{bmatrix} \Delta \theta \\ \Delta U / U \end{bmatrix}$$

$$M_{ij} = U_i U_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij})$$

$$M_{ij} = -U_i \sum_{\substack{j=1 \\ j \neq i}}^N U_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij})$$

$$L_{ij} = -U_i (G_{ij} \sin \theta_{ij} + B_{ij} \cos \theta_{ij})$$

$$L_{ij} = \sum_{\substack{j=1 \\ j \neq i}}^N U_j (G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij})$$

Higher R/X in MGs

$$M \approx 0; L \approx 0$$



$$\Delta U / U = N^{-1} \Delta P$$

$$\Delta \theta = K^{-1} \Delta Q$$



## Relationship between Voltage Deviation and Power Increment in DC-MGs

Different from AC-MGs, the line of DC-MGs is only of the resistance characteristics

$$\begin{bmatrix} \Delta P_1 \\ \Delta P_2 \\ \dots \\ \Delta P_4 \end{bmatrix} = \begin{bmatrix} N_{11} & N_{12} & \dots & N_{1n} \\ N_{21} & N_{22} & \dots & N_{11} \\ \dots & \dots & \dots & \dots \\ N_{n1} & N_{n2} & \dots & N_{nn} \end{bmatrix} \begin{bmatrix} \frac{\Delta U_1}{U_1} \\ \frac{\Delta U_2}{U_2} \\ \dots \\ \frac{\Delta U_n}{U_n} \end{bmatrix} \Rightarrow \Delta U / U = N^{-1} \Delta P$$

This paper:

Thus,  $\Delta U$  are mainly related to  $\Delta P$  in the AC-MGs and DC-MGs

The EVs are used as active power units to regulate the bus voltages





# Outlines

1

Introduction

2

Relationship between voltage and power  
incensement in AC&DC-HMG

3

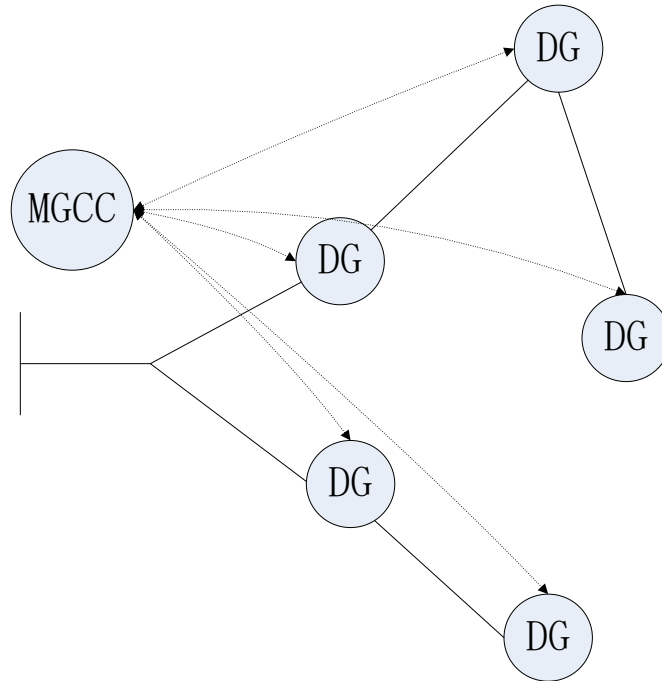
Distributed voltage regulation algorithm

4

Simulation results and discussion



## Centralized algorithm



**1. Central controller.**

**2. High communication burden.**

**3. Communication period is longer.**

**4. Lower expandability.**

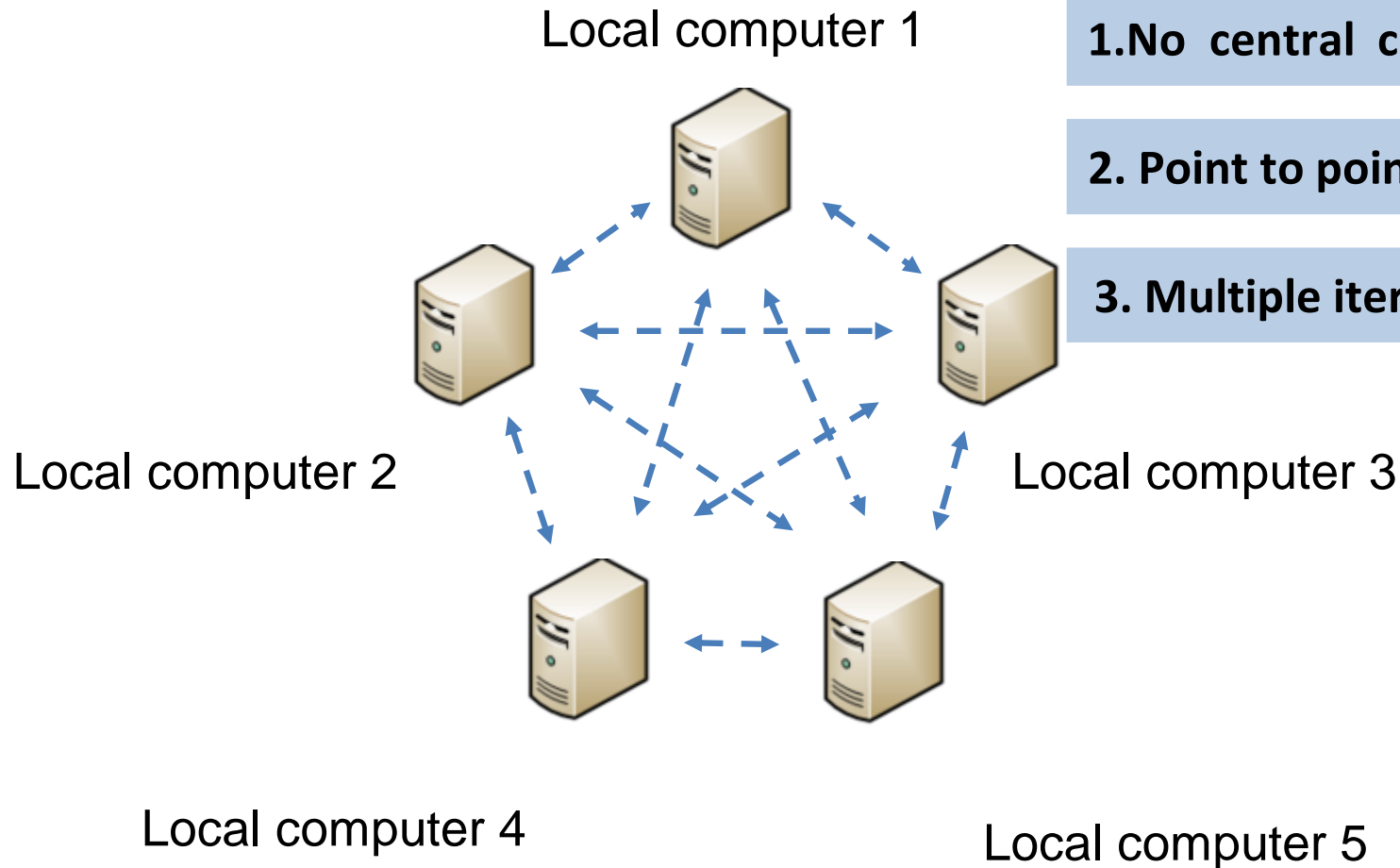


## Decentralized algorithm - Gossip Algorithm

1. No central controller

2. Point to point

3. Multiple iterations





## Objective Function

$$\min F = \sum_{i=1}^N (\Delta U_i)^2 = \sum_{i=1}^N (U_i(\Delta P) - U_{\text{REF}})^2$$

Diagram illustrating the objective function components:

- $\Delta U_i$  is labeled as **voltage deviations**.
- $U_i(\Delta P)$  is labeled as **voltage magnitudes**.
- $\Delta P$  is labeled as **power increments**.

$$s.t. \quad U_{imin} \leq U_i \leq U_{imax}$$

$$\Delta P_{imin} \leq \Delta P_i \leq \Delta P_{imax}$$



## Solution of the Proposed Model

$$\begin{array}{ll} \min & F(x) \\ \text{s.t.} & g_j(x) \geq 0, j = 1, \dots, m \end{array}$$

By the penalty function method

$$F' = F + \mu \sum_{i=1}^M (\min\{0, g_i(x)\})^2$$



$$x^* = -H^{-1}c$$



optimal solution

quadratic function



$$F' = \frac{1}{2} x^T H x + c^T x$$





## Solution of the Proposed Model

$$H = \begin{bmatrix} \frac{\partial^2 F'}{\partial x_1^2} & \frac{\partial^2 F'}{\partial x_1 \partial x_2} & \cdots & \frac{\partial^2 F'}{\partial x_1 \partial x_n} \\ \frac{\partial^2 F'}{\partial x_2 \partial x_1} & \frac{\partial^2 F'}{\partial x_2^2} & \cdots & \frac{\partial^2 F'}{\partial x_2 \partial x_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^2 F'}{\partial x_n \partial x_1} & \frac{\partial^2 F'}{\partial x_n \partial x_2} & \cdots & \frac{\partial^2 F'}{\partial x_n^2} \end{bmatrix}$$

&

$$c = k^U U + k^P P + k^C C$$

constant matrices

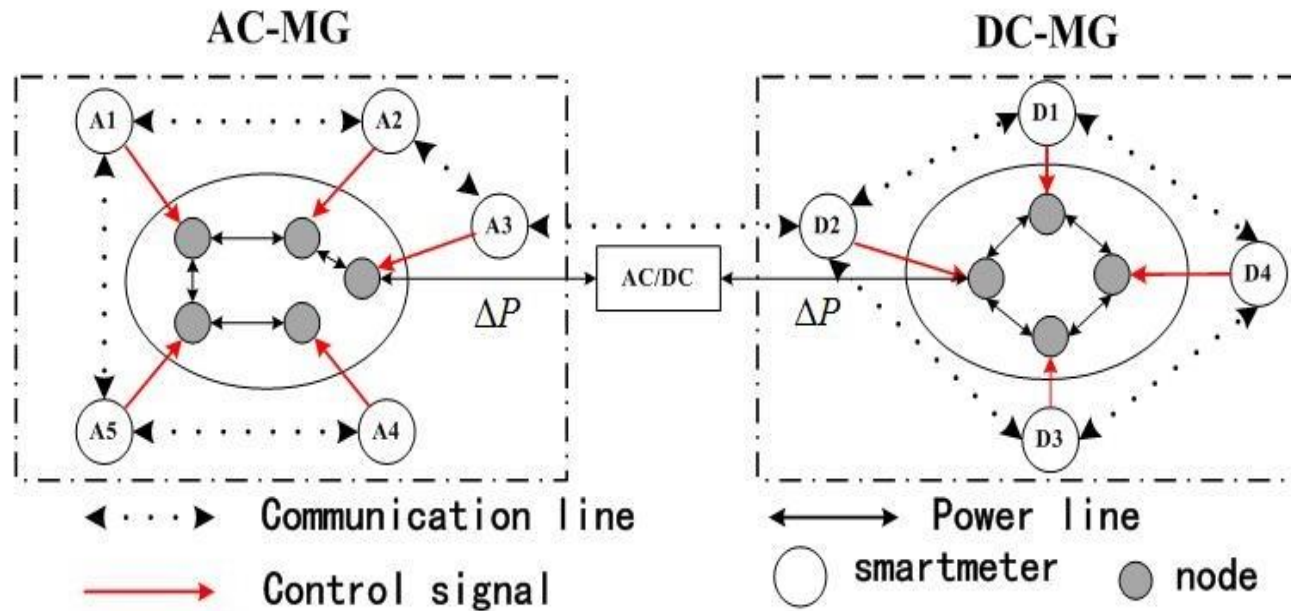
$$x^* = -H^{-1}c$$



$$x^* = \Delta P_i^* = \sum_{j=1}^N H_{ij}^{-1} (k_{ij}^U U_j + k_{ij}^P P_j + k_{ij}^C C_j)$$



## Distributed Voltage Regulation Strategy for AC&DC-HMG



Voltage regulation processing : ♦ Internal regulation



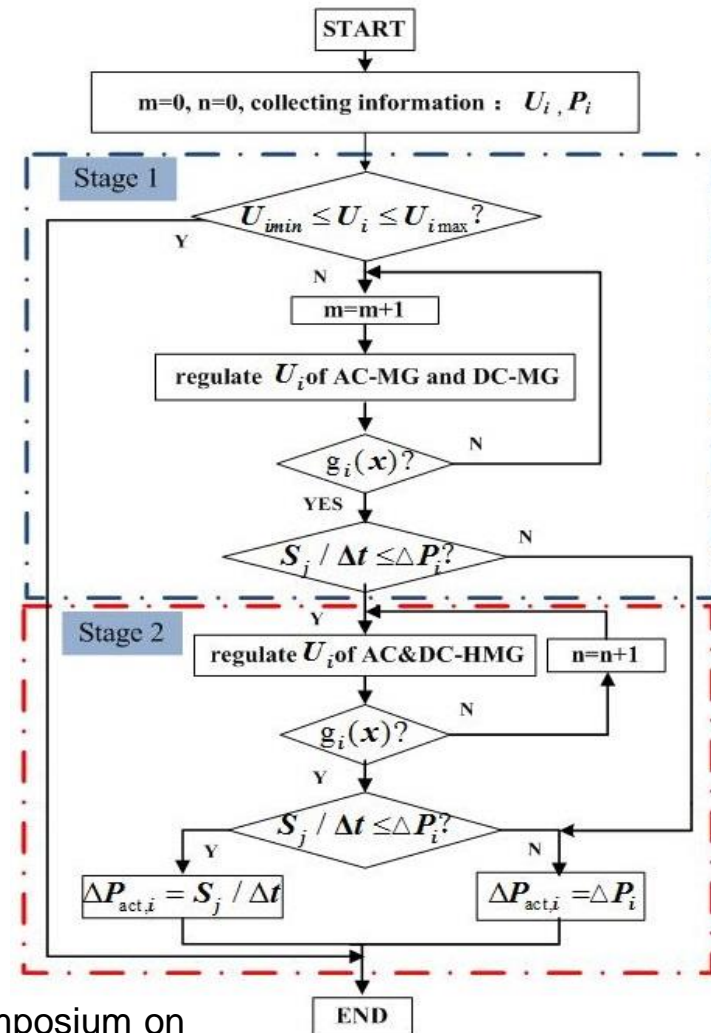
♦ unified regulation



## The whole voltage regulation processing

**Stage 1:** Each MG regulates its voltages by distributed voltage regulation algorithm.

**Stage 2:** There are six cases of the second stage voltage regulation.





## Six cases of the second stage

### Six cases of the second step

Scenarios	AC-MG voltages	EVs' scheduling capacity	AC-MG voltages	EVs' scheduling capacity
Case 1	$\leq 5\%$	----	$\leq 5\%$	----
Case 2	$\leq 5\%$	Enough	$> 5\%$	Not enough
Case 3	$\leq 5\%$	Not enough	$> 5\%$	Not enough
Case 4	$> 5\%$	Not enough	$\leq 5\%$	Enough
Case 5	$> 5\%$	Not enough	$\leq 5\%$	Not enough
Case 6	$> 5\%$	Not enough	$> 5\%$	Not enough

Different cases correspond to different solutions.



# Outlines

1

Introduction

2

Relationship between voltage and power  
incensement in AC&DC-HMG

3

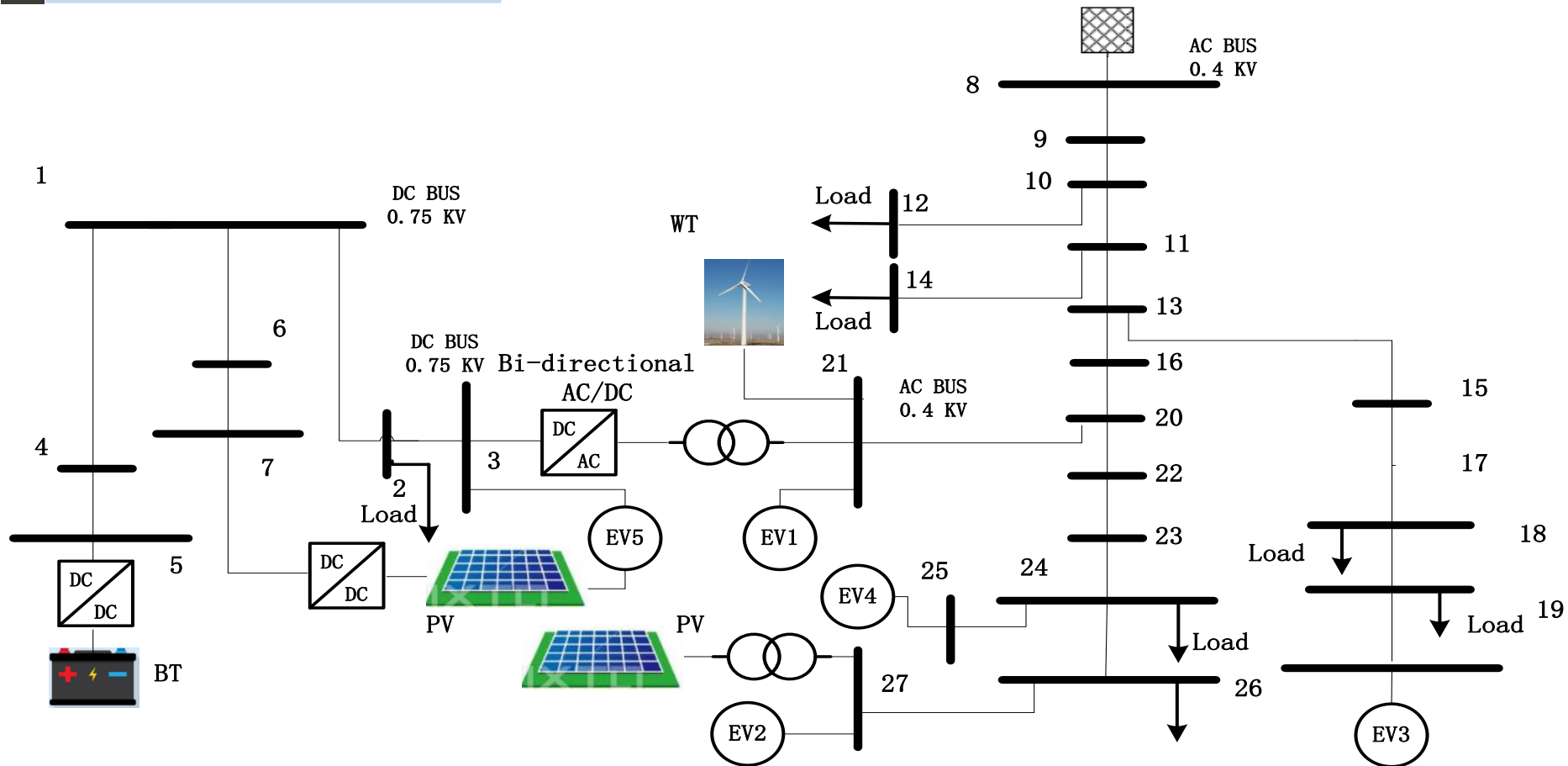
Distributed voltage regulation algorithm

4

Simulation results and discussion



### Microgrids topography



### Parameter setting

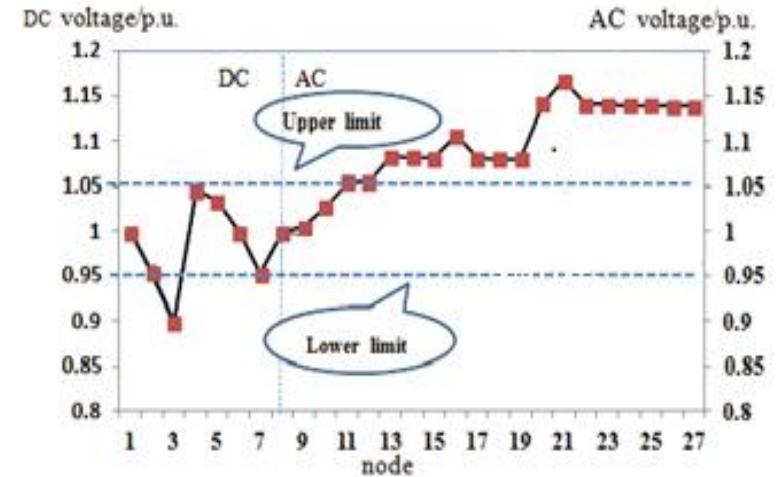
TABLE II. MAXIMUM CONTROLLED EVS POWER

Controllable Component	Maximum power to be dispatched/MW
EV 1	$\pm 0.61$
EV 2	$\pm 0.79$
EV 3	$\pm 0.96$

TABLE III. ACCESS POWER OF EACH NODE

Node	Active power/MW
Node 2 (load)	0.45
Node 5 (BT)	-0.5
Node 7 (PV)	0
Node 12 (load)	0.00575
Node 14 (load)	0.01395
Node 17 (load)	0.0091
Node 18 (load)	0.00605
Node 21 (WT)	0.62
Node 27 (PV)	0

### Initial voltages

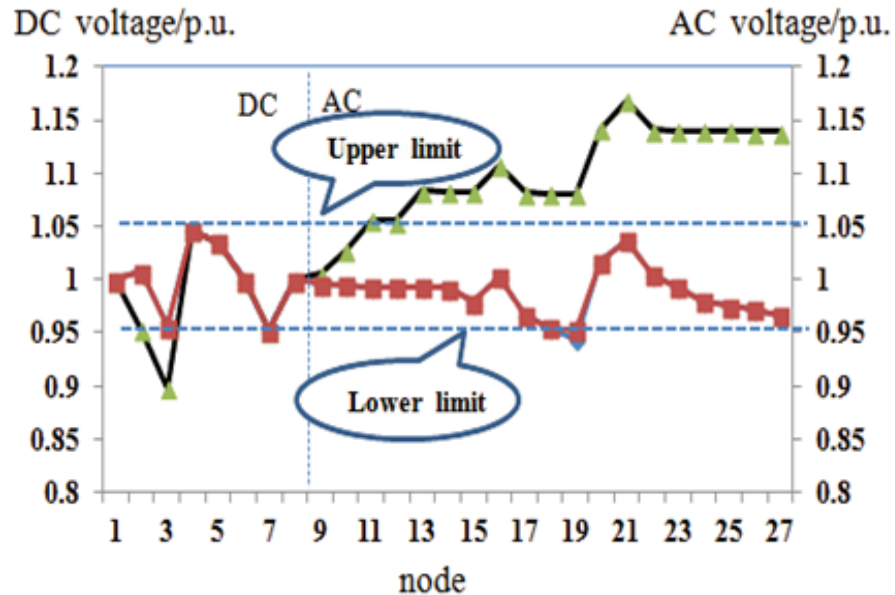


The initial voltages of AC-MG and DC-MG are mostly over limits





### Case 1



After voltage regulation for the first stage, the voltage fluctuation is within  $\pm 5\%$

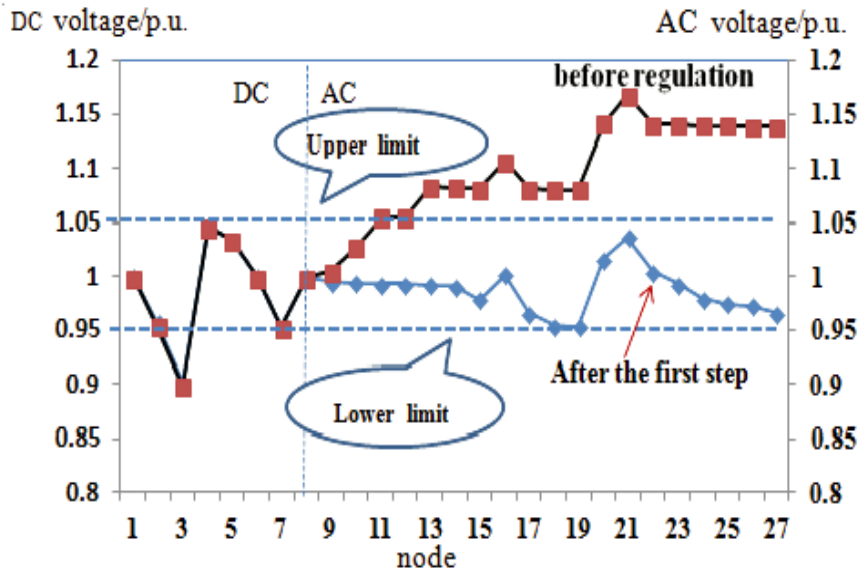
$$\Delta P_{EV1} = -0.1843MW$$

$$\Delta P_{EV2} = -0.1056MW$$

$$\Delta P_{EV3} = -0.95MW$$



## Case 2

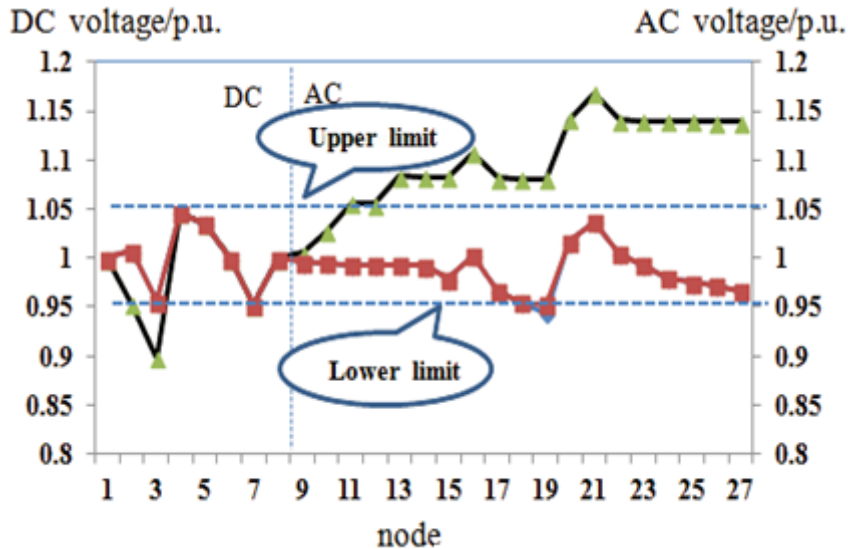


After the first stage regulation, the node voltages are still mostly over the limits in DC-MG.

The solution of case 2 is launched.

Case 2\*

### Case 2\*



By using the scheme for case 2, the voltage regulation coordinated within AC-MG and DC-MG for the second stage is launched.

### Optimal power of EV nodes

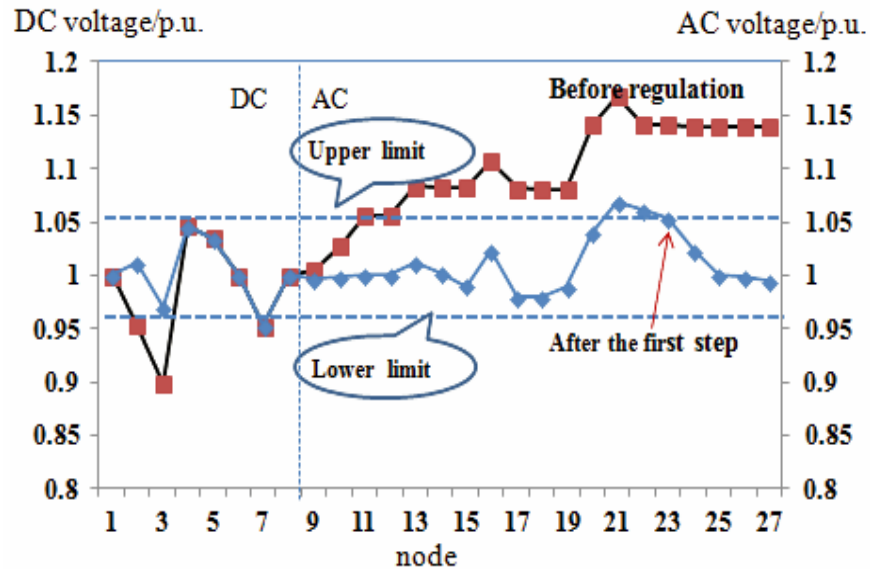
$$\Delta P_{EV1} = -0.8041MW$$

$$\Delta P_{EV2} = 0.0931MW$$

$$\Delta P_{EV3} = -0.4550MW$$



## Case 4



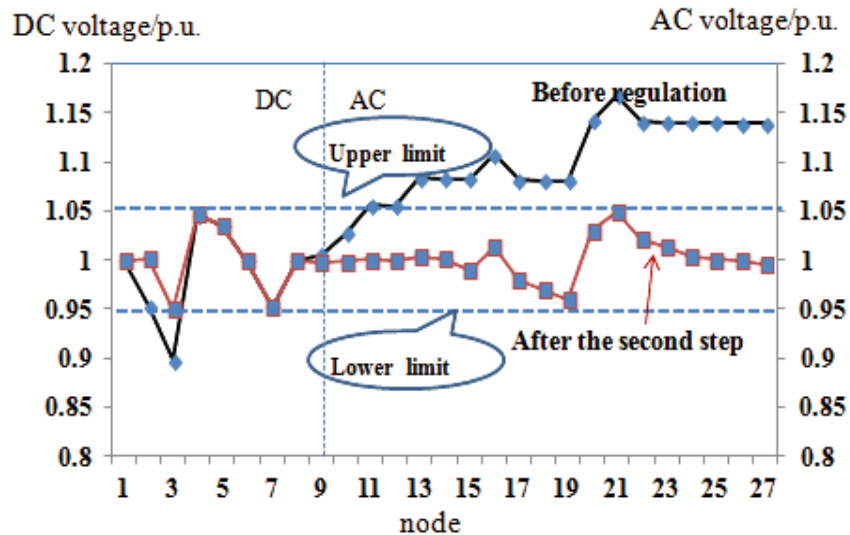
After the first voltage regulation stage, there are still some node voltages over the limits in AC-MG.

The solution of case 4 is launched.

Case 4\*



### Case 4\*



By using the scheme for case 4, the voltage regulation coordinated within AC-MG and DC-MG for the second stage is launched

### Optimal power of EV nodes

$$\Delta P_{EV1} = -0.1355MW$$

$$\Delta P_{EV2} = 0.00956MW$$

$$\Delta P_{EV3} = -0.1566MW$$



## Conclusions

- By the proposed method, the voltage deviation of the AC&DC-HMG can be stabilized within 5% with power coordination between AC-MG and DC-MG with EVs connected the related nodes.
- In addition, each node regulates its voltage based on communication only within neighboring nodes, thus reducing the burden for communications.

## Future works

- We only considered the grid connection situation, and did not consider the situation when the EVs was connected in the island mode.
- The scheduling of electric vehicles can be optimized.





# Thank you!